DOCUMENT RESUME

ED 075 236

· 京京 0.15 962

TITLE INSTITUTION Elementary Mathematics: A Handbook for Teacters. Alaska State Dept. of Education, Juneau. Office of Fublic Information and Publications.

PUB DATE HOUSE

Aug 71 33p.

EURS FRICE DESCRIPTORS MF-\$0.65 BC-\$3.25

*Curriculum: *Curriculum Guides: *Elementary School

Mathematics: *Individualized Instruction;

*Instruction; Instructional Materials; Laboratory

Procedures: Mathematics Soucation

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The aim of this quide is to aid elementary teachers in individualizing instruction. Eight general objectives of teaching mathematics are listed, 11 topics are identified as being the scope of elementary mathematics, a one-page mathematics curriculus flow chart for grades 8-8 is provided, student and teacher needs and evaluation are discussed in general terms, and three examples of individualized instruction are given. A section on mathematics laboratories includes directions for four activities along with a short list of math lab materials and books. A bibliography of 32 references on mathematics education is given. (DT)



Elementary Mathematics

G 015 962

ALASKA DEPARTMENT of EDUCATION, BIVISION of INSTRUCTIONAL SERVICES, August, 1971

ELEMENTARY MATHEMATICS

A Handbook For Teachers



I'M AN INDIVIDUAL!

Dr. Manhall Lind Commissioner of Education

Dr. W. Roseff Jones Direction of Instructional Services

2971

ACKNOWLEDGEMENTS:

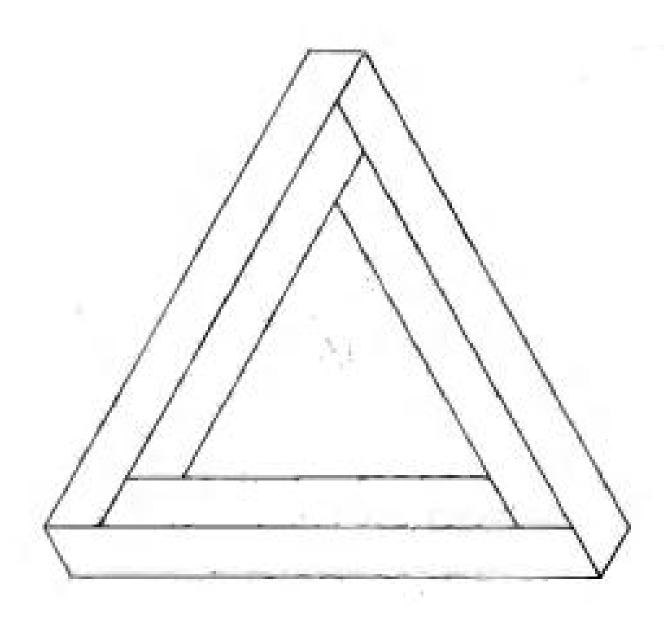
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TABLE OF CONTENTS

- W Philosophy
- 2 General Objectives of Teaching Mathematics
- 3 Seems
- 4 Computers Flow Chart.
- 5 Implementation
- 5 Evaluation
- 7 Examples of Individualized Instruction
- 17 Mathematics Laboratory
- 15 Resources for Learning
- 20 Math Laboratory Materials
- 21 Appendix
- 25 Bibliography
- 27 The Mysterious Block



- 88

ERIC

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Philosophy

Education, to be living and effective, must be directed toward familiarizing children with these ideas which will enable there to function in the custant world and develop in them the capacities which will prepare them for the future. This involves skills and processes of thought that are important tocally as well as mathematically. These skills must be developed tully and to the maximum extent commensurate with a child's stillity. This development must liste place in each child, not just in a majority of the children.

This corriculum guide is prepared to aid teachers in accomplishing the goal of individualization. An individualized mathematics program will be achieved through an evolutionary process. Some of the principles that guided the committee toward the individualized instring concepts are as follows:

- I. The child is the main concern of the teacher.
- 2. The child becomes a partner in the teaching learning process.
- Each child's positive settlimage is enhanced by his successful experience in an individualized learning situation.
- A child can perceive the beauty of the structure of mathematics.

It is our hope that this guide will be useful to individual teachers and to local committees. Even though some sections of this guide include specific examples, we nealize that individualized instruction will take on a semewhat different nature from one classroom to the next.



Personing the BEAUTY

General Objectives of Touching Mathematics

- I. To develop in the child the responsibility to gian his program of instruction, to evaluate it, and to exquire the drive to eccomplish these goals.
- 2. To recognize and cultivate the inherent potential and creativity in each child.
- 3. To provide a firm foundation in the basic mathematic skills and principles.
- To make mathematics relevant to the individual and useful in his daily encounters with the society.
- 5. To develop a logical, sequential method of reasoning.
- 5. To onable a child to perceive the beauty of the structure of methematics.
- 7. To enable a child to enjoy recreational mathematics.
- 8. To looter in the child an understanding and use of mathines in computation.

Scope

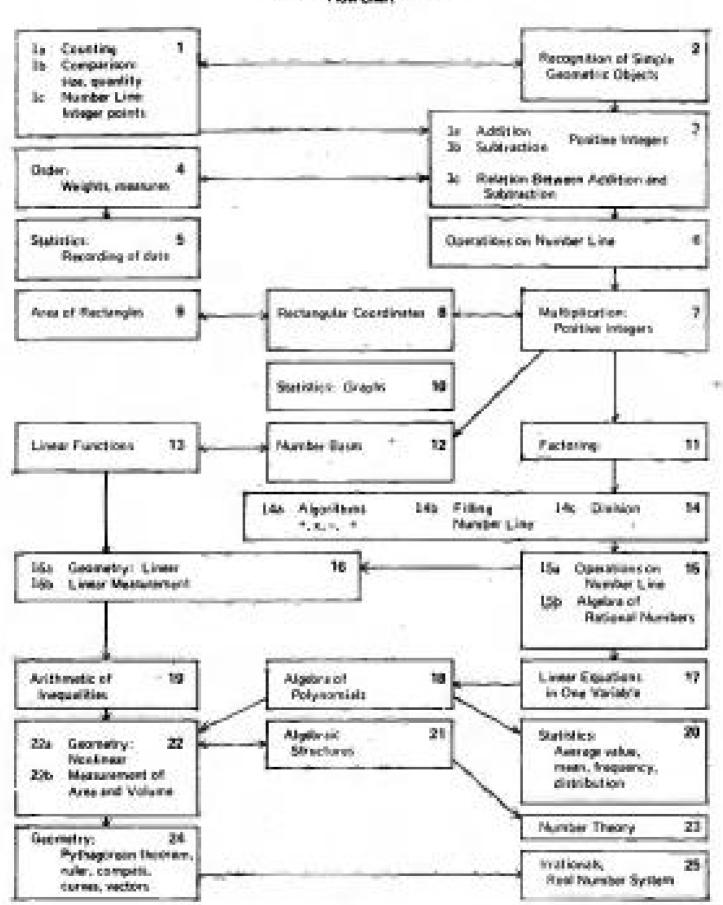
Mathematics in the elementary school is concerned with various aspects of the structure of reathematics. The teaching-tearning sequence in mathematics can be likewed to the placing together of a series of jig-ten postles. One may begin with any piece, but each puzzle shows a picture of the entire structure. The earlier learner is given large pieces simple in outline and color. The more advanced learner is given smaller pieces more inegular in outline and richer in color.

The scope of elementary mathematics includes the following topics. (These topics are NOT in a sequential order nor receiverily disjoint.) See appendix for richards cope.

Numbers and Operations
Special Topics
Functions and Graphs
Geometry
Sets
Number sentences and Solutions:
Measurement
Statistics and Probability
Problem Solving
Application of Mathematics
Lopical Thinking



MATRICURRICULUM K-6 Flow Chart



İmplementation

findividual differences dictate individualized learning. The committee feels that this is the basis for all educational experiences. Individualization may cause a change in the educational philosophy of an individual teacher or, possibly, of a whole school system.

Individualized instruction must meet the needs of both the child and the teacher. Son.; of the child's needs are:

- 1. To feel that the subject matter is relevant to him.
- 2. To have immediate verification of his work.
- To see property in his program.
- To accept the responsibility for learning.
- 5. To here open lines of communication with the teacher.
- 5: To gain recognition among his peets.

Some of the teacher's needs are:

- To realize that a new, complete physical outlay is not necessary, individualization can be accomplished with the existing books of varying difficulty.
- 2. To have the idea of individualised instruction understood by the children.
- To recognize that the teacher and each child may have to move into the program gradually, developing individual responsibilities, as they work together toward individuality in learning.
- To have open lines of communication.
- To determine the child's level.
- To develop a method of evaluating the chit/s progress. (The committee feels that this
 is best reported by a progress report retirer than a standard report need.)
- . 7. To improve his subject matter compagence to meet the needs of every individual.
 - To realize that the tracker is now on a one-to-one correspondence with the pupil, even though he may be working with small groups or total class sections, individualization of instruction does not mean isolation. As opportunity for group action and reaction is necessary.



Doubsettion

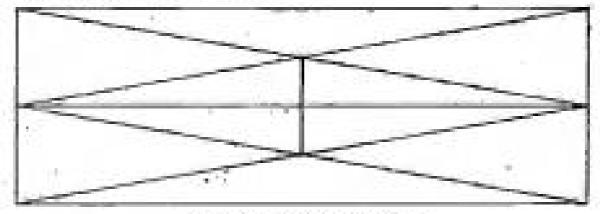
The changing role of the feacher is most evident in the approach to the evaluating process. The time proviously spent in lecturing in a traditional classroom situation will now be spent in managing student progress and in stimulating the flow of ideas. Some factors involved in evaluation are:

- T. Informal testing to too tractor-made problems covering basic contests.
- Teacher observation—does the student work confidently and accurately?
- Teacher-child conferences conversation invelving retrieving, use of measurement, entireties, etc.
- 5. Format diagnostic testing
- Since children are at differing stages of development, we must evaluate that mathematical experience of each child to determine his starting level.

A continuous appreisal of the child's progess is necessary to help him move from concept to concept and from one level to another. The progress record least by the child and the teacher is as excellent tool to encourage the child's self-directed resthematical growth and to help him determine his own meds. This record is very useful in reporting the child's progress to his perents.

Evaluating the school curriculum is also part of the total evaluation. This will be a continuing process of measurement and of judgment to we compare the school's curriculum to the current objectives that we wish to accomplish in the mathematics program. Even a first-grade child can answer questions such as: Do you like math? What part do you like best? What did you learn in math? What would you like to learn next? What part was most difficult?

Curriculum evaluation should involve parents, administrations, teachers and children. Teachers, parents and administrators will be able to assess the correlation between objectives and the curriculum, but only the child can supply the answers as to how meaningful the methodology program has been to him.



How many triangles can you count?

Examples of Individual Land Instruction

Before describing a typical math class, it should be emphasized that individualizing instruction is by nature very personal. Each teacher will find a unique way of individualizing depending on his personality and that of his class members.

The following models are examples of individualized classroom instruction which are affectively being used today in Alaskan schools.

Market A.

This model evolved from a need to adapt teaching methods to a mobile student population; to give each child the maximum learning opportunities while he was in the group. The model his been used sustantially from primary through junior high leads.

The teacher has informally evaluated the child and has devised a possible approach for this child at his level.

To begin the program a very simple concept, such as sets, is introduced to the extire class. Many will already be familiar with sets; informal discussion and demonstration by the children will occur. Several copies of basic texts, grade levels 1 = 8, will be readed to meet individual differences.

Astign each child extensi on the concept at his level or one level below. There will usually be two or three children working at the same level. As each solves his problem, he compares his work with others in his group, discussing methods, solutions, etc. He may need help from someone who has finished that level of instruction, thus he asks a friend to assist the group or to help him individually. As shildren work, frequent discussions occur with the problem illustrated on the overhead projector or the chalchourd. The entire class usually because involved in the instruction several times during the work period.

The teacher is the expeditor, moving casually from group to group, never helping unless an individual or group carved solve their problem independently.

With many levels of difficulty of the concept being discussed and illustrated, the children may see immediate application of the concept. The children working at lower levels may especially benefit from the discussion. A child may join another group and work through problems at several levels as he becomes more expert at using the concept to solve problems, or he may work. Even, checking with others as he progresses. If a child discovers a really stimulating idea he should be encouraged to pursue if further even if it branches out from the original concept.

An individual progress report for that concept is stapied to a large folder. As the child sectoralisty completes several problems and compares them with his contemporaries, he checks off his progress and deposits his paper in his folder. If he is not ready for the rest

sevel. The group he has joined will either help here master difficult points or tall him he useds more practice before he is neetly in move forward with them. (The teacher can "expedite" at this point.)

Each child works at his own rate. As he mode to know he asks, and is instructed individually by other children or the teacher in small group interaction and in discussions invating the entire class. Children may be working from a level of manipulating objects, performing simple operations with sets or using sets to solve problems with positive and negative integers. Each concept has such a broad range of application and leads to easily to the need for other concepts that the individual child controls his own requestial development in the program.

The teacher constantly assesses each child's performance as the moves around the room, impowing where the child is working and his rate of progress Papers are available in each folder for re-checking. More evaluation occurs as the teacher asks each child to work one or two problems at his level and to discuss the operation with her. Formal betting at his level may be used at intervals if the teacher feets it is necessary.

More than one series of texts should be used so the children are familiar with several methods of presentation. This heigs the children discover many methods of problem solving. Formulating and solving problems of their own is a most desirable learning situation.

hydinidualiting is a social process and carriot take place when each child is working strictly by himself. These must be fine recovered of students among groups to enable communication of differing ideas and approaches. The teacher must also move constantly, drawing out students, attractions the flow of ideas and giving problem tolking situations to encounting children to apply mathematical concepts to real-life situations. Frequent group discussions must take place to stimulate the entire cites.

Salf discipline develops as the child sees himself as an individual, learning in an individual way, yet involved in the process of assisting others to learn. Children are sharing the enjoyment of mastering skills and understanding concepts. They are learning to work in groups, developing a respect for the opinions of others, and practicing many other aspects of becoming effective citizens.

Model 8

litedist B is a type of individualized instruction that a lifting-ade teacher in Alaska has been using for several years. She has developed a method that works well for her. It is our hope that many of her ideas will be useful to you in your classroom.

The class starts when the student recreivny returns the daily work and quistes. Each student has already checked and corrected with green percit his daily work before turning it in. It is reassuring to know the teacher has glanced over the paper and can quickly correct any revious error before it becomes a set habit. As some as a student has filled yesterday's matin work, he can given at his individual progress sheet on the front of his folder imade

proviously by the fraction! to see where he should begin finling.

It is not uncommon for the math ability range in the class to be time or four grade levels. The teacher avoids pre-judging a child's potential which may have been latest under a conventional teaching system. Although she has no more than an average mathematical background, she has confidence in her own ability to help the child determine his starting point. She finds individualizing her math class is easier since acquiring many supplementary math books and aids to fit this wide ability range.

The atmosphere in this observors is one of student freedom to talk and move around the room. One of the reasons the teacher is so apportolic toward this method of teaching is because her discipline problems with the children have nearly disappeared, in a setting where every student is chall-god to work at his own individual rate and level, each student, is able to superience success. This success builds positive attitudes in the students, which may carry over to their offspring in a few short years.

She believes many small discussion groups and some full class discussions are an essential part of any method of inclinidualizing instruction. She insists that understanding of math concepts in an important aspect of learning which some children may not get unless these concepts are developed and repeated in small and large discussion groups. Some children learn, much more quickly from hearing another student's explanation than from the teacher's explanation. The teacher is also aware that the most always take time to list in to each individual.

There is no set schedule of inclinitual study time, small group study time or large group discussion time. She feets one of the real rewards of individualization in the openness with which her students discuss their particully progress, innights and difficulties with classmates and with her. This is in contrast to the conventional situation where a teacher may feel hopelessly frustrated because a student is completely preference.

An outstanding feature of this instruction is the reger attitude each child shows toward his mathematics. Sume students may not cover too much proved during a given period of time. However, with this feeling of eageness, learning is taking place.

Students want to be personally involved in what littly are doing, and Thill method of individualizing mathematics is an excellent way for each student to discover material that is uniquely suited to him as an individual.

Medel C

The notice of individualised learning pervades the instructional method one teacher has used over the past ten years in methematics and science at the traditional wearsh, eighth and sinth grade levels.

This narrative describes more clearly the conduct of a class at the minth grade level. The implementation may vary considerably depending upon the maturity of the individuals

awaived and make-up of the climit, but the general notions and ground rates apply at all levels.

Every response to a given of astroom stimulus should be governed by a consideration of these questions.

- I is it the best line of action for the student?
- 2. Wall it contribute to the making of a responsible citizen?
- Wild it leter here with the learning process of other people?
 (We do not have the right to interfere with another's learning process.)
- 4. Will it result in an unsectnoury contest between teacher and student?

With every student there must be a continuous program of self-evaluation and goal setting. With older students this can be quite objective and straightforward (i.e., why are you in this class? what would you like to go back and ne-do? etc.) but with younger children this procedure might become more exploratory, with a gradual lifting and sorting, before realistic pools are established.

Generally, the greater the topply of resource material the better, but these classes have functioned well with just one textbook series until other materials were accomplated.

First must be spent throughout the year to stinforce the notion that each person can and will learn. When the youngster accepts this notion and a starting point with a realistic goes has been established, the teacher can then relax his grip and let the student proceed along his learning path—working, stabiling, and receiving from activities with his classmates.

This working-helping phase might wall be a very quiet period; but then, again, if could be noisy. Caution: Do not be hasty to judge, as degenerative, activity among a group of students. Very often a burst of laughter accompanied by back-singuing can indicate that someone is the group "his finally seen through." A group of students may seek permission to go observers (they specify where) to study together when they feel the resulting activity will lead to a disruption of the class as a whole, e.g., when they wish to view single concept himstrips or movies, or to practice fundamentals.

What about letting the student use his study time to prepare for a test in another subject for next period? By all means! When the young person is functionally mature enough to be open with you, you have a lot going for you; and it that stage of development, discipling problems begin to disappear!

The conventional notion of grades needs to be modified to that each child is graded on his own progress (along several evenues to be discussed later) and that work is the sole requirement for in "everage" grade. Expect sparts in performance as he proceeds along his learning path.

Beyond this "seerage" grade, a subjective judgment of "attitude toward the class" is woven into the labric of the evaluation. (Note: This takes into openideration such things as:



alitenterises, late arrivals, working relation with classmates, willingness to explore and excit. If DGES NOT INCLUDE attitude of student toward the tracker. Teaching is not a populating contest. The teacher should expect and encourage differences when opinions are sized in an open atmosphere. Differences of opinion should not be interpreted as an insuff by an individual.)

High in priority on the flet of student needs is immediate serification of bar work.

The need is fulfilled in three years.

- 1. Consensual validy flors, great to profit. Typical is, "I got this. Where-oit?"
- Access to the teachers' edition textbook.
 A ratio of one book to teven students seems edequate. (Notes to the teacher in the text). It are very helpful to the child.)
 - p. For use in school during the day.
 - b. To take home nights and weekends. Post a definite schedule when each child can have a book on one night of each week. He can then organize his study time in other subjects around this.
- Access to the teacher. Atthough it may not be possible in all situations, the teacher should be available to assist any time during any reasonable hour. This helps to convey the idea that the teacher is concerned with and interested in the progress of the child.

The nord for each rield to see progress.

- 1. Must have access to the record book the longer called the "grade" book (
 - To check his own progressment to determine a new starting point.
 - .b. To assist in recording his own work. Question: Can you trust the child to record accurately? Yes, especially when harming rather than teaching is the goal. A prevening attitude of, "Who are you readly killding!" becomes quite commonstate.
- Student Work Sheets (tests) at the option of the student. Single concept work sheets encompassing a depth in understanding are always meliable. Students take these when they feel they are ready.
- 3. Teacher Evaluation (tests) at the option of the teacher. A currulative work sheet opering the work done by any and all of the students may come at any time. All children may not finish this work sheet (test) in the time allowed. Caution it is difficult to use a work sheet such as this and not discourage some children. An attitude of "I'll do all I can" must preselt. The evaluation also includes rendom checks of papers and observations made during the study work time.

Note: All these evaluations (Wills) are considered to be learning devices and are treated as such. When learning is stressed, there seems to be a tendency to study to learn rather than study to pass lists and, at that time, if becomes unnecessary to goard against sheeting.

There is a wend for a counting board or "feedback" puch by both seather and child. (Understand "feedback" to carry this maining, a means to improve the fidelity of the violent.) This implies a DVNAMIC SYSTEM IN CONSTANT CHANGE!

Student evaluation forms carry three evenues of questioning on both subject matter and citizenship. These evenues are provided to:

- Explore the shild's progress.
 - a. As he expects himself to be moving along.
 - b. As he would like to be doing.
 - As his school and community expects him to be doing.
- Bive an opportunity for re-intablishing doals.
- Give an opportunity for comment and constructive criticism.

The student's rale becomes one of having control over his own progress. He can explane, probe and experiment both horizontally and vertically over a wide area. Caution: Do not be disturbed if a child goes back to raido work done at an earlier time because, perhaps now, he finds a read for greater understanding.

A vital role in this entire process is the feacher's recognition of himself as a professional person who livess such child somewhere within his own target area. The teacher assists when needed and redirects when the child has gone too far affekt.

The teacher should make an effort not to interfere in a learning process of a child. Time is required for tives processes to take place. The teacher should letter hands out of the bearing experiment until he is asked to easist or until he sees the child headed for a blind alley from which the child cannot extricate himself.

The teacher may be compared to a flywheel, absorbing the excess energy and then feeding it back as the reads of each individual child dictate.

The teacher is called upon to render climical judgment in many simultaneous situations. Mistakes will be made. Errors in judgment become immediately recognizable and remediate action to possible while the fearning process continues.

Priority should be given to preparing substitute teachers. On one occasion, the shidner provided the key to satisfying the requirements of a rejustant substitute who demanded a

definite set of lesson titlers before he would accept the job. One boy volunteered, "Each of us can just write down what we plan to be doing for the next ten days and give him that." The teacher handed his substitute a sheaf of papers (one for each child) for each class, and departed. The substitute distitutly checked each sheet on each child for the first two or three days and then, happily, found he could spend his time more productively assisting the children in their learning activities.

The question of discipline divisity community. A purishable offense is one in which someone interfers in the learning process of another. This is a relatively rare offense, When there is some doubt is to what a best of activity might meet, the question. "Are you happened" or "What are you supposed to be doing?" solves a lot of problems. When a child is restless and can't seem to get an with the table at hand, he can always straighten books on the back said. Generally, the discipline problems that do occur are minor corepored to those of the old lock-step classroom.

How does the teacher place a child at his test working level and how does he make sure that, the child moves along at a satisfying rate?

Several devices can be used to achieve this purpose. They include:

- Standardized test results from the previous spring.
- iii. Observation of a chalkboard gares played with single, hardwrestel arithmetic concepts. This game is much like the old-fashiored spelling bee and is held once a week, with the losers supplying ice cream to the minners at the sed of each grading aeriod.
- Individual and group conferences with the child in which he assesses himself.
- 4. Carrent evaluations and worksheets.

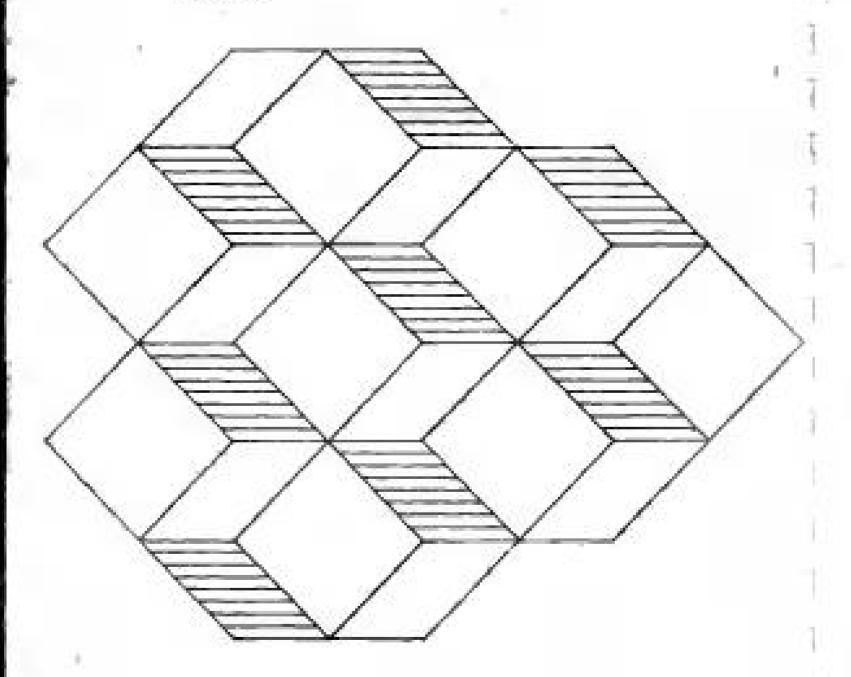
If the child it new to the school, refer to the evaluation given by his previous become However, the leacher may prefer to observe the student for himself because a child change from day to day. He should be a better-organized individual today then he was yesterday. If this does not appear to be the case, then, the leader had better for Lord wher.

ASSESSMENT OF THE CHILD SHOULD BE CONTINUOUS.

In turningry.

- The conventional notion of grading it not compatible with an individualized fearuring situation.
- The child must have control over his learning propriet.
- Each third should understand that he is expected to do als best and that he well by judged on his progress.

- There can be NO learning contest between the learner and the child.
- It is vital that the teacher recognite his role as a professional police who keeps EACH, child somewhere within his own target ares.
- Teaching can be satisfying and rewarding WHEN THE EMPHASIS IS PLACED ON LEARNING.





de

Mathematics Laboratory

The laboratory approach to feathing can play an important role in the child's understanding of mathematics. The materials may be pupil constructed, teacher constructed, or commercial.

The respectals should be readily evallable to that the student may use them at any time. This may be in a corner of the classroom, or possibly in the media room.

The laboratory learning progresses from the concrete to the abstract concept(i) as the children work with the materials

Some exemples of laboratory situations follow:

Areas of closed prometric figures

Materials: 1" or rob pages, scinors.

Objection: The student will discover the majoring of area, develop a method of finding the area, and poster solution formulas.

Procedure. The student will cut I' squares from the graps paper, and use them to construct a square. By counting the number of squares he will find the area. Using the same method, he will proceed to the area of other figures, rectangles, triangles, and irregular frame.

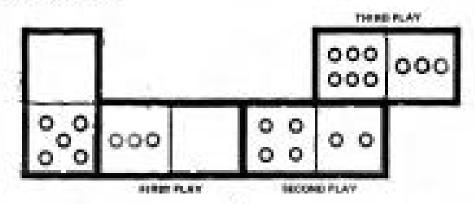
There will be countless solutions by the students. As a group they will then compare, and evolve solitable conclusions.

Deservices:

Margarith. Double oine dortinos.

Objective: To gain proficiency in the use of multiplication facts.

Procedure: The students play the game by placing the dominos and to and so the total of the two symbols equals a multiple of a given number. In the following it instruction, the answers are multiples of 4.



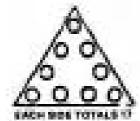


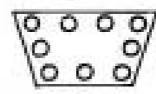
Magic Triangle

Aliaberia (c. Posterboard and colored paper disca which are consecutively numbered.

Objectives. To gain skill in addition facts.

Procedure: Give the students a magic triangle. Then encourage them to make up their own magic figures. Below are examples from a fifth grade class.







EACH SIDE TOTALS 18

Survivati

Historials: Catalog and newspapers.

Objections: Computational dellis and restoring

Proorders: There is an uninhabited island at ____ Latitude. It has no man-made facilities. With 3 or 4 friends, plan what suggitts and equipment you will need to survive on the island for the month of July.

The only source for ordering equipment and supplies is the mail order datalog and grocery addition the newspaper.

You have unlimited money, but can only ship 1,000 gounds of materials to the island. List by name of item, shipping weight in pounds and ounces, and the price.

the abto to justify your use of each item. If another group successfully challenges its usefulness, you must drop that item and as a penalty drop one other item of your choice. (Very by changing time limit, latitude, seaton, or by imposing a monetary limit, etc.)

Freeters to Learn by Edith Biggs, published by Addison-Wesley, confeins valuable information and practical examples for leachers planning to implement a math laboratory.

See Recourses for Learning section for a partial list of mate aboutony materials. Page 19.

Resources for Learning

A rich, stimulating environment facilitates learning. This encompasses many types of necourage e.g., human resources, firsthand observation and experience, exploratory and experimental material, opportunities and materials for self-expression, printed materials, audio-visual materials and never learning media.

- Aliman resources including the children, people from the governmenty, parents, other teachers, . . .
- Firechard abstractions and experiences has the learner had crithmetic experiences outside of the classroom that he day there with the class? Is he appear boy? Has he built things with his dad? Or does the teacher need to build these experiences? Can he collect the money and lesso the records for the classroom book club? Can the class visit the grocery store? the bank? etc.
- Opportunities and materials for self-expression verbalization through discussion, sole playing, students fulloring other students, student-made tests, problems and systems created by students, student-built models, charts, maps and scale drawings, self-established goals.
- Printed materials textbooks and supplementary texts at varying levels, backs on the history of mathematics, readiness booklets, excidenced booklets, reexpapers tettlevaluation materials and meaningful practice materials designed for use by the child without direction by the teacher, exercises to give math practical applications to the child's delig life, use of measurement, objects, optical Kestons, geometric designs, open-andered sequences and patterns, possible and consentrums.
- Audio-cissal meterials blocks, flavorel board, counter board, games, flash certs, abacus, rocks or marbles to help inscribe numbers, clocks, toy money, cherts, individualized computational skills hits, programmed learning kills, overhead projectors, tapes, films, filmstrips, records, computers, tolerision, commercial games, (See bibliography printed in November, 1956, Arithmetic Feether.) Some of the best aids are teacher made.



Math Laboratory Materials

inexpensive Lab Items.

Developmental Meth. Cards, Sets A-L. @ 3.95/set = Addison-Wesley Fig.

Methematics Laboratory = \$15.00 = published by Book = Leb, Inc., 1449 1744 St., Brooklyn, New York 11218 - Kill No. 3044

Multiplying Machine — published by Selective Educational Equipment, Inc., 3 Bridge St., Newton, Manachuretts

Tri-Ominos - Pressesan - existable Northern Commercial Co., Anchorage, Alacka

Quible — Parker Bros. — 3D Tic Tac Toe — available Roberts, Mt. View, Ataska (or try your local toy store and hobby shop.)

The Minning Touch Sum Fun Smartu

Equational for games—souththe Allesta Sphool Schools - Anathrough, Abedia

Cross Number Putities — Ideal Number Rummy - Kenwarthy Ed. Servicet Make One — Dutch Haleidoscope Puzzles — Ideal

Augistra From Waste School Supply

Cribbage — Thrifty Drug Store, Mt. View, Alaska
Dominios — Thrifty Drug Store, Mt. View, Alaska
No to your leaf to store and holds dead
Number — Cross Number Stame, Roberts, Mt. View, Alaska

Books:

Fun with Putrier — Joseph Leeming
Zers is Zillians — Irwin Wetts (Scholadic Book Services, 904 Sylvan Ave., Englewood:
Cittle, New Jersey 07628)
Arithmetic Gener & Activities — Wagnes, Haster & Gillieby
Wetten stics Gener for All Guides — Lole J. May

Regilets of: An Accounted Sibhiography of Suggested Manipulative Devices for the lab may be obtained by writing to PERCY. 650 International Amport Rt., Anchorage, Alaska 99503.



APPENDIX

Topics of the Scape expanded:

Number and Operations

Place Value Motation **Materal Numbers** Whole Numbers Profession . Rational Numbers Real Mumbers Bases Other Than 10 Ranic Principles Aligorithms. Number Line: Cardinal and Ordinal Number Theory - Primes, Even and Oast, Etc. Pattern Recognition. Computational Short Cuts Multiple Operations Mydalar Arithmetic

Minicurement.

Relegation of Shapes and Forms.
Building a Conceptual Framework of the Notion of Measurement Concepts of Length, Anna, Volume, Weight Estimating and Reserving OH!
Systems of Measuring Units
Money
Time
Temperature
Concepts of Liquid — Cups, Pints, Quarts, Galloro Batio and Proportion

Statistics and Probability

Miles and

By introducing Statistics and Probability theory early, we are giving the student a charge for a higher level of sophistication with which to interpret what he sees in ordinary life.

Sets

Sample Spaces and Events Compound Events Statistical Probability Mathematical Expectation Conditional Probability

Functions and Graphs

Note: A function is a relation between two sets.

Ordered Pairs. Graphing Inequalities Graphing of Solution Sets

AUGUS

Coardinate Geometry

Number Line

Bar and Circle Graphs

Pictographs Maps and Charts Scale Drawing Line Greats

Problem Solving

Wester:

Logical problem solving is a primary function of elementary

methematics.

Graphs, Scale Drawings, Diagrains

* Estimation : Average

Noverlitten Solution Seti

Application to Real-Life Situations

Ratio and Proportion

Translation from Number Sentences to Short Stories, and

Vice Veru Multiple Operations

And the second second

Number Line

Applications to Other Disciplines



Geometry (Informal, Nonmetric)

Recognition of Shapes and Forms
Number Line
Points, Lines, Planes, Simple Closed Curves:
Solids
Coordinate Geometry
Congruence
Pythagorean Theorem
Panallel, Perpendicular, Transverse
Spatial Relationships
Constructions
Symmetry
Formal Attention to Abolized Concepts
Topology

Applications of Mathematics

Vocational
Commercial
Recreational
Personal
Physical Environment
Other Areas of the Curriculum

Sett

Element Equivalent Sets Non-Equivalent Sets Cerdinal Number Subset **Ore-to-One Matching** One-to-Mary Matching Number Fair Empty Set Selution Set Union Intersection. Miniversal Set Venn (Euler) Diegram Sets in Geometry Probability and Statistics. Cartesian Product Disjoint Sets. Partitioning.

Logical Thinking

Truth Tables
Assigns and Theorems
Formal and Informal Proofs
Quantifiers (all and some)
Negation
Conjunction (and)
Disjunction (or)
Conditional and Bi-Conditional Statements (id., thefi-)
Converse, Inverse, and Contrapositive
Industries and Deductive Reasoning
Patterns and Sequences
Use of Logic in Developing New Concepts
Informal Logic in Computation and Problem Solving

Number Sentences and Solutions

Addition
Subtraction
Multiplication
Division
Notation
Decimals
Haltonals
Variables
Constants
Open and Closed Sentences
Solution Set

Special Topics

History of Mathematics
Use of Computational Aids
Absolute Value ...
Determinants
Trigonemotric Ration
Paper Folding
Modular Anthonolic
Other Bases
Artificial Operations



Elis Rography

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The two piece cube

Explain how this cube is constructed.
If may be taken apart and prived together without breaking.
The back faces look like those visible.



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FLEMENTARY MATHEMATICS ...

Dr. Me-that L. Linel Epiterwisioner of Education

Office of Public between and Fundaments Alters Department of Education August, 1971

